Physical characteristics of LaCr$_x$Al$_{1-x}$O$_3$: DFT approach

H. Javid$^a$, S. A. Aldaghfaq$^b$, M. K. Butt$^a$, S. Mubashir$^a$, M. Yaseen$^{a,*}$, M. Ishfaq$^a$, S. Saleem$^a$, H. Elhosiny Ali$^{c,d}$, H. H. Hegazy$^{c,d}$

$^a$Spin-Optoelectronics and Ferro-Thermoelectric (SOFT) Materials and Devices Laboratory, Department of Physics, University of Agriculture Faisalabad 38040, Pakistan

$^b$Department of Physics, College of Sciences, Princess Nourah bint Abdulrahman University, P. O. Box 84428, Riyadh 11671, Saudi Arabia

$^c$Research Center for Advanced Materials Science (RCAMS), King Khalid University, Abha 61413, P. O. Box 9004, Saudi Arabia.

$^d$Department of Physics, Faculty of Science, King Khalid University, P.O. Box 9004, Abha, Saudi Arabia.

The magnetic, electronic, and optical properties of Cr doped LaAlO$_3$ are examined by Full Potential linearized augmented plane wave (FP-LAPW) method within Density functional theory (DFT). The pure compound (LaAlO$_3$) is doped with different concentrations of chromium (Cr) to examine the doping effects on its characteristics. The calculations of band structure (BS) and density of states show Cr has major contribution while La, Al and O atoms have little involvement in the states near Fermi level. The magnetic features revealed that Cr plays major participation in ferromagnetic nature of LaCr$_x$Al$_{1-x}$O$_3$. The results of electronic and optical revealed that the compound under study is suitable for spintronics and optoelectronics applications.

(Received March 28, 2022; Accepted July 1, 2022)

Keywords: DFT, Spintronics, doping, Perovskite materials

1. Introduction

Perovskite oxides have obtained significant attraction of scientist around the globe because of their unique characteristics like ferromagnetism, superconductivity, multiferroicity and colossal magnetoresistance [1-4]. All these properties make these materials exclusive for industrial and technological uses including memory devices, optoelectronics, solar cells, and transducers [5-7]. In recent years, diluted magnetic semiconductors have obtained much consideration due to their applications in spintronics devices [8,9]. Moreover, induction of ferromagnetism in nonmagnetic Perovskites compound is significant from experimentally and theoretically prospective because of spin functionality addition to host crystal [10-13]. In addition to this, multiferroic compounds are being obtained by doping of transition metal (TM)[14]. The TM ions exhibit intrinsic functionalities such as superconductivity, ferroelectricity, thermoelectricity, and magnetism [15,16].

Lanthanum Aluminate is most promising candidate in the family of perovskite oxides from theoretical and experimental point of view [17]. This compound has high value of dielectric permittivity, which is beneficial for different application like ferroelectric thin film microwave devices, high frequency capacitor and dielectric resonators [18]. When we introduce doping in intrinsic LaAlO$_3$, it has been found that the compound become suitable for manufacturing of eye safe laser as well as optical communication devices [19,20]. Moreover, the chromium doped LaAlO$_3$ formulated by solid state reaction have shown suitability for vivo imagining applications [21]. Benam et al. investigated pressure effect on optical features of LaAlO$_3$ by first principle which stated that the value of band gap (E$_g$) increasing by increasing compression on system [22].

* Corresponding author: myaseen_taha@yahoo.com

https://doi.org/10.15251/JOR.2022.184.481
Boudali et al. observed the elastic, electronic, thermal as well as structural features of LaAlO$_3$ and declared that this material is appropriate for optoelectronic applications [23].

In present work, the optical, magnetic, and electronic features of Cr doped LaAlO$_3$ compounds have been analyzed by DFT. In electronic properties, BS, DOS and PDOS are calculated to observe the nature of material along with participation of elements. In optical properties, different parameters such as optical conductivity ($\sigma (\omega)$), reflectivity ($R (\omega)$), absorption coefficient ($\alpha (\omega)$) dielectric constant, extinction coefficient ($k (\omega)$) and refractive index ($n (\omega)$) are computed. The magnetic properties are also examined to check the magnetic behavior of the material. There is no previous theoretical work on magnetic, optical, and electronic calculations of Cr doped LaAlO$_3$ that encourages us to analyze its properties. Our calculated outcomes are beneficial to implement this compound for spintronics and optoelectronic applications.

2. Method of calculation

The FP-LAPW method within DFT applied in Wien2k code is utilized to examine the optical and electronic behavior of Cr doped LaAlO$_3$ [24,25]. The wave function, charge density and potential are extended on two bases in FP-LAPW method. It can be observed that potential and wave function are expanded on spherical harmonic basis inside atomic sphere whereas plane waves are extended outside the atomic sphere. The potential in both areas can be explained by following relation:

$$V(r) = \left\{ \begin{array}{ll}
\sum_{LM} V_{LM}(r) Y_{LM}(\theta) & \text{inside sphere} \\
\sum_{k} V_{k} e^{iK \cdot r} & \text{outside sphere}
\end{array} \right.$$

(1)

All constraints are precisely determined in the Hamiltonian of multiple body system by eliminating conversion association potential [26, 27]. The value of $l_{\text{max}}$ is constant outside the sphere, whereas its value is taken as 10 inside the sphere. The 33 k-point sampling is utilized to make 1000 Monkhost pack meshes grid. Moreover, RMT(muffin tin sphere radius) values utilized for La, Al, O and Cr atoms are 2.26, 1.51, 1.51 and 2.4 (a.u), respectively. The value of $G_{\text{max}}$ =14 is used for atomic radii conversion. The LaAlO$_3$ possess cubic structure having space group of Pm-3m (221). The atoms of La are centered at (0.5, 0.5, 0.5), the Al are positioned at (0, 0, 0) whereas the three oxygen are situated at (0, 0.5, 0), (0, 0, 0.5) and (0.5, 0, 0) in crystal unit cell of LaAlO$_3$. When Cr is replaced at aluminum site in LaAlO$_3$, the atom is located at (0, 0, 0) in unit cell. The atomic radius is 2.50, 1.84, 2.00 and 1.52 (Å) for La, Al, Cr and O, respectively. The computed lattice parameters values for this compound are 3.79 Å. The electronic configuration of elements is [Ne]$3s^2 3p^1$ for Al, [Xe]$5d^6 6s^2$ for La, [Ar]$3d^4 4s^2$ for Cr and [He]$2p^6 2s^2$ for O.

3. Results and discussions

3.1. Electronic properties

The electronic behavior of Cr doped LaAlO$_3$ based on BS, TDOS as well as PDOS are calculated with different concentrations of Cr doping as represented in Figs. 1-4. These properties are examined for LaCr$_x$Al$_{1-x}$O$_3$(x=0.125, 0.25, 0.50, and 0.75) and are computed in first Brillion-zone. The distance between VB maxima and CB minima gives value of $E_g$. It was examined that when we change doping concentration in LaAlO$_3$, the $E_g$ varies improperly. The nature of $E_g$ was determined as direct and indirect (see Fig. 1(a)) for LaCr$_{0.125}$Al$_{0.875}$O$_3$ in spin up ($\uparrow$) and spin down ($\downarrow$) channel, respectively. When LaAlO$_3$ was doped with 0.25 and 0.50 concentration of Cr, the $E_g$ was calculated as indirect in both spin regions. Furthermore, the $E_g$ value for LaCr$_{0.25}$Al$_{0.75}$O$_3$ was observed as 0.22 and 0.05 eV (see Fig. 1(b)) in spin down ($\downarrow$) and spin up ($\uparrow$) channels, respectively. For LaCr$_{0.50}$Al$_{0.50}$O$_3$, the value of $E_g$ (see Fig. 1(c)) in spin up ($\uparrow$) and down ($\downarrow$) region...
was 0.34 and 2.65 eV. Moreover, behavior of $E_g$ was computed as direct in spin up ($\uparrow$) and indirect in spin down ($\downarrow$) channel for LaCr$_{0.75}$Al$_{0.25}$O$_3$ (see Fig. 1(d)).

Fig. 1. BS of Cr doped LaAlO$_3$ (a) LaCr$_{0.125}$Al$_{0.875}$O$_3$ (b) LaCr$_{0.25}$Al$_{0.75}$O$_3$ (c) LaCr$_{0.50}$Al$_{0.50}$O$_3$ (d) LaCr$_{0.75}$Al$_{0.25}$O$_3$.

Fig. 2. TDOS of Cr doped LaAlO$_3$ (a) LaCr$_{0.125}$Al$_{0.875}$O$_3$ (b) LaCr$_{0.25}$Al$_{0.75}$O$_3$ (c) LaCr$_{0.50}$Al$_{0.50}$O$_3$ (d) LaCr$_{0.75}$Al$_{0.25}$O$_3$. 
Fig. 3. Atomic TDOS of Cr doped LaAlO$_3$ (a) LaCr$_{0.125}$Al$_{0.875}$O$_3$ (b) LaCr$_{0.25}$Al$_{0.75}$O$_3$
(c) LaCr$_{0.50}$Al$_{0.50}$O$_3$ (d) LaCr$_{0.75}$Al$_{0.25}$O$_3$.

Fig. 4. PDOS of Cr doped LaAlO$_3$ (a) LaCr$_{0.125}$Al$_{0.875}$O$_3$ (b) LaCr$_{0.25}$Al$_{0.75}$O$_3$ (c) LaCr$_{0.50}$Al$_{0.50}$O$_3$ (d) LaCr$_{0.75}$Al$_{0.25}$O$_3$. 
All computations of BS showed semiconductor behavior of compound under study. Moreover, we have computed electronic properties of LaAlO₃ in our previous research and found a band gap of 3.46 eV in its pure form [28].

The PDOS and TDOS for LaAlO₃ are computed at various concentrations of Cr (see Figs. 2-4). It can be seen in Fig. 4(a), for LaCr₀.₁₂₅Al₀.₈₇₅O₃, the contribution of La-5d and Cr-3d is maximum in CB, whereas O-2p states have shown highest participation in VB in spin up (↑) and down (↓) channel. According to pseudo potential theory, the bond length decreases with the elevation in hybridization strength, and both these parameters plays significant role in electronic BS formation [29]. Hybridization strength between 2p(O) and 5d(La) is maximum at all concentrations of Cr in LaAlO₃. When LaAlO₃ is doped with Cr at (x = 0.25 and 0.50), the Cr-3d and La-5d states coincide with Fermi level in CB whereas the involvement of O-2p is maximum as shown in Fig. 4(b & c). For LaCr₀.₇₅Al₀.₂₅O₃ compound, the influence of Cr, La and O states have dominating effect in conduction and VB for spin down (↓) and spin up (↑) channel, respectively.

3.2. Optical properties

The optical features of Cr doped LaAlO₃ can be observed in terms of conduction, absorption, dispersion, reflection, and polarization. The absorption and dispersion of electromagnetic radiation are observed by dielectric function which is schematically shown in Fig. 5(a & b). The dielectric constant and BS are directly related with each other. Moreover, the atoms interactions with incident photons are computed by frequency dependent dielectric constant. It contains real and imaginary part and can be expressed by the following relation [30]:

$$\varepsilon(\omega) = \varepsilon_1(\omega) + i\varepsilon_2$$

(2)

The $\varepsilon_1(\omega)$ displays the polarization of light while the $i\varepsilon_2(\omega)$ is directly linked to absorption of incident light and electronic BS. Different optical properties such as $\sigma(\omega)$, $k(\omega)$, $n(\omega)$, $\alpha(\omega)$, and $R(\omega)$ are examined from imaginary part $\varepsilon_2(\omega)$ of dielectric function. The $\varepsilon_2(\omega)$ can be analyzed by the computations of BS using following relation:

$$\varepsilon_2(\omega) = \frac{e^2h}{\pi m^2\omega^2} \sum_{vc} \int |n, n'(k, q)|^2 \delta[\omega_{n,n}(k) - \omega] d^3k$$

(3)

The $\varepsilon_1(\omega)$ can be examined from the $\varepsilon_2(\omega)$ with the help of Kramers-Kronig relationship [31]:

$$\varepsilon_1(\omega) = 1 + \frac{2}{\pi} \int_0^\infty \frac{\omega' \varepsilon_2(\omega')}{\omega'^2 - \omega^2} d\omega'$$

(4)

The extreme values of $\varepsilon_1(\omega)$ appear at 4.7, 4.61, 4.6 and 5.06 eV for LaCrₓAl₁₋ₓO₃ at x= 0.75, 0.50, 0.25, 0.125, respectively (see Fig. 5(a)). However, the highest value of $\varepsilon_1(\omega)$ for pure LaAlO₃ is 5.26 eV [28]. After reaching at highest point, the values of $\varepsilon_1(\omega)$ have shown fluctuations in high energy region because of variable transition rates. The imaginary part displays material ability to absorb light. The computed values of $\varepsilon_2(\omega)$ are represented in Fig. 5(b) and maximum values of LaCrₓAl₁₋ₓO₃ at (x=0.125, 0.25 0.50, 0.75) occurs at 7.58, 7.83, 7.83 and 8.31, respectively.
Fig. 5. (a) \( \varepsilon_1(\omega) \) (b) \( \varepsilon_2(\omega) \) (c) \( R(\omega) \) (d) \( \alpha(\omega) \) of Cr doped LaAlO\(_3\) 

The reflectivity is one of the most significant phenomena which described the features of compound to the falling light. The \( \varepsilon_1(\omega) \) values of dielectric function and \( R(\omega) \) displays the similar behavior. When the photon energy elevates, the reflectivity also elevates. The highest value of reflectivity (see Fig. 5(c)) occurs at 8.73, 8.63, 8.88 and 9 eV for LaCr\(_x\)Al\(_{1-x}\)O\(_3\) whereas \((x = 0.125, 0.25, 0.50, 0.75)\), respectively. The peaks appeared due to the inter-band transitions among valence and CB. The \( R(\omega) \) can be computed by using formulation:

\[
R(\omega) = \frac{[n(\omega) - 1]^2 + k^2(\omega)}{[n(\omega) + 1]^2 + k^2(\omega)}
\]

The \( k(\omega) \) and \( n(\omega) \) are linked with one another through \( \alpha = \frac{4\pi k}{\lambda} \). The absorption of incident light lies in UV region (see Fig. 5(d)) which originates from 4 to 10 eV. The maximum absorption appears at 9.66, 9.77, 9.90 and 8.98 eV for 0.125, 0.25, 0.50 and 0.75 doping of Cr in Lanthanum Aluminate. Thus, the absorption of ultraviolet frequency is highest in this energy region which describes that this material is active in given energy range. The extinction coefficient of Cr doped LaAlO\(_3\) is computed, and the respective results are shown in Fig. 6(a). No changes are observed in \( k(\omega) \) values at 0 eV but changes with increments in amount of incident light. The maximum peak occurs at 1.66 for LaAlO\(_3\) without doping which is reported in our previous calculations [28]. The \( n(\omega) \) explains the propagation of light inside the compound, and it can be explained by the expression:

\[
n(\omega) = \left( \frac{[k^2(\omega) + \varepsilon_2(\omega)]^{\frac{1}{2}} + 1}{2} \right)^{\frac{1}{2}}
\]
The $\varepsilon_1(\omega)$, $\varepsilon_2(\omega)$ and $n(\omega)$ displays almost similar behavior, and these functions are related with each other through $\varepsilon_1(\omega) = n^2 - k^2$ and $\varepsilon_2(\omega) = 2nk$. The values of $n(\omega)$ are maximum at 5.089, 4.638, 4.981 and 4.76 for LaCr$_x$Al$_{1-x}$O$_3$ ($x= 0.125$, $0.25$, $0.50$, $0.75$), respectively which is shown in Fig. 6(b). The bond breaking in the compound appears in relation to the electromagnetic radiations and it gives information about $\sigma(\omega)$. The $\sigma(\omega)$ of Cr doped LaAlO$_3$ is represented in Fig. 6(c). It can be seen that maximum values of $\sigma(\omega)$ for Cr doping of 0.125, 0.25, 0.50 and 0.75 at 7.67, 8.49, 8.78 and 8.33, respectively.

### 3.3. Magnetic properties

The total, interstitial and individual magnetic moments are calculated by PBE-GGA [32]. To study the probable magnetism origin and effect of various spins, the results of different Cr concentration doping in LaAlO$_3$ are summarized in Table 1. The effective magnetic moments of LaCr$_x$Al$_{1-x}$O$_3$ at 0.125, 0.25, 0.50 and 0.75 is 3.00014, 3.00029, 3.00025 and 3.10847 $\mu_B$ respectively. It can be observed that highest magnetization occurs at $x= 0.50$. The magnetic properties of Cr doped Lanthanum aluminate depends upon direct exchange interaction. The direction of spin alignment can be indicated by sign of magnetic moments of various atoms. A negative magnetic moment of different atoms exposes anti ferromagnetic or ferromagnetic interaction whereas the positive sign value shows the spin alignment in the same direction [33]. The values of magnetic moment of Cr, Al, La and O atoms has opposite signs at all doping concentrations, which disclosed that all the atoms interact in ferromagnetic order. It is well reported from the magnetic outcomes of LaCr$_x$Al$_{1-x}$O$_3$ that the compound is ferromagnetic in nature.
Table 1. Calculated $M_{\text{int}}, M_{\text{La}}, M_{\text{Cr}}, M_{\text{Al}}, M_{\text{O}},$ and $M_{\text{Tot}}$ in units of $\mu_B$ for Cr doped LaAlO$_3$ compound.

<table>
<thead>
<tr>
<th>$x$</th>
<th>$M_{\text{int}}$</th>
<th>$M_{\text{La}}$</th>
<th>$M_{\text{Cr}}$</th>
<th>$M_{\text{Al}}$</th>
<th>$M_{\text{O}}$</th>
<th>$M_{\text{Tot}}$</th>
</tr>
</thead>
<tbody>
<tr>
<td>0.125</td>
<td>0.44869</td>
<td>0.01103</td>
<td>2.32365</td>
<td>0.00121</td>
<td>0.0228</td>
<td>3.00014</td>
</tr>
<tr>
<td>0.25</td>
<td>0.13868</td>
<td>0.00462</td>
<td>0.79543</td>
<td>-0.00081</td>
<td>0.07577</td>
<td>3.00029</td>
</tr>
<tr>
<td>0.50</td>
<td>0.49281</td>
<td>0.040333</td>
<td>2.26073</td>
<td>-0.00108</td>
<td>0.08357</td>
<td>3.00025</td>
</tr>
<tr>
<td>0.75</td>
<td>0.29688</td>
<td>-0.05787</td>
<td>2.67061</td>
<td>0.00236</td>
<td>0.18506</td>
<td>3.10847</td>
</tr>
</tbody>
</table>

4. Conclusions

In this work, the magnetic, optical, and electronic properties of Cr doped Lanthanum aluminate are computed by FP-LAPW method. It is observed that Cr doped LAO is semiconductor in both spin channels. Inter-band transition depends on the doping of Cr element. The DOS plots have shown major involvement of Cr-3d, La-5d and O-2p. Meanwhile, various optical parameters such as $R(\omega), \alpha(\omega), n(\omega), k(\omega)$ and $\alpha(\omega)$ are examined. Moreover, the computations of magnetic properties confirmed the ferromagnetic nature of LaCr$_x$Al$_{1-x}$O$_3$. All the results of Cr doped LaAlO$_3$ indicates the suitability of this compound for potential uses in optoelectronic and spintronics devices.

Acknowledgements

The authors extend their appreciation to the Research Center for Advanced Materials Science (RCAMS), King Khalid University, Saudi Arabia, for funding this work under grant number KKU/RCAMS/G011-21. The authors also express their gratitude to Princess Nourah bint Abdulrahman University Researchers Supporting Project number PNURSP2022R81, Princess Nourah bint Abdulrahman University, Riyadh, Saudi Arabia.

References

[23] Z. Ali, I. Khan, I. Ahmad, M. S. Khan, S. J. Asadabadi, Materials Chemistry and Physics, 162, 308-315 (2015); https://doi.org/10.1016/j.matchemphys.2015.05.072
[33] Z. Ali, I. Khan, I. Ahmad, M. S. Khan, S. J. Asadabadi, Materials Chemistry and Physics, 162, 308-315 (2015); https://doi.org/10.1016/j.matchemphys.2015.05.072
[38] B. Amin, I. Ahmad, M. Maqbool, S. Goumri-Said, R. Ahmad, Journal of Applied Physics, 109(2), 023109 (2011); https://doi.org/10.1063/1.3531996